

MATHEMATICS

Stage 5

Number and Algebra, Algebraic Techniques

Distributive Laws

Number and Algebra, Equations

Linear

Number and Algebra

Indices

Number and Algebra, Linear Relationships

Cartesian Plane

Teacher: Kyall Duncan

Exam Equivalent Time: 39 minutes (based on allocation ~1.25 min/mark)



Worked Solutions

1. **D** Linear (227339) **Core A**

If $x = -2$,

$$2(-2) - 3 = -7$$

$$4(-2) + 1 = -7$$

$\therefore x = -2$ satisfies both.

$\Rightarrow A$

2. **B** Indices (002644) **Path B** **HSC**

$$\begin{aligned} \frac{6x^2y}{3} \div \frac{2y}{5} &= \frac{6x^2y}{3} \times \frac{5}{2y} \\ &= \frac{30x^2y}{6y} \\ &= 5x^2 \end{aligned}$$

$\Rightarrow A$

ALGEBRA TIP: When you divide by a fraction, invert the divisor and multiply as shown in the Worked Solution.

3. **A** Cartesian Plane (010503) **Path C** **HSC**

$$2x - 3y = 8$$

$$3y = 2x - 8$$

$$y = \frac{2}{3}x - \frac{8}{3}$$

$$m = \frac{2}{3}$$

$$\therefore m_{\text{perp}} = -\frac{3}{2} \quad (m_1 m_2 = -1 \text{ for } \perp \text{ lines})$$

Equation of line $m = -\frac{3}{2}$ through $(2, 0)$:

$$y - y_1 = m(x - x_1)$$

$$y - 0 = -\frac{3}{2}(x - 2)$$

$$y = -\frac{3}{2}x + 3$$

$$2y = -3x + 6$$

$$3x + 2y = 6$$

$\Rightarrow B$

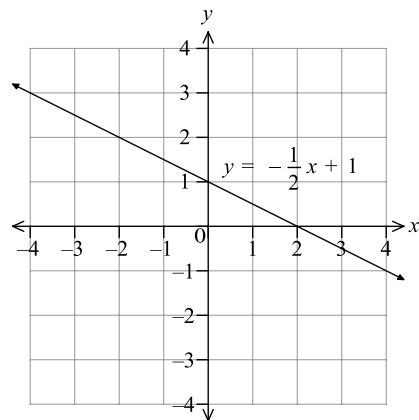
4. **B** Cartesian Plane (228191) **Core B**

$$y - 1 = -\frac{1}{2}x \Rightarrow y = -\frac{1}{2}x + 1$$

$$y\text{-intercept} = 1, \text{ gradient} = -\frac{1}{2}$$

x -intercept occurs when $y = 0$:

$$0 = -\frac{1}{2}x + 1 \Rightarrow x = 2$$



5. **B** Cartesian Plane (228429) **Path C**

$$(2, -3), (-5, 4)$$

Using the distance formula:

$$\begin{aligned} d &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(2 - (-5))^2 + (-3 - 4)^2} \\ &= \sqrt{49 + 49} \\ &= \sqrt{98} \\ &= 9.899\dots \\ &= 9.9 \text{ units (nearest tenth)} \end{aligned}$$

6. **B** Indices (226565) **Path C**

$$\begin{aligned} \frac{6\sqrt{3} - \sqrt{5}}{2\sqrt{5}} &= \frac{6\sqrt{3} - \sqrt{5}}{2\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}} \\ &= \frac{\sqrt{5}(6\sqrt{3} - \sqrt{5})}{2 \times 5} \\ &= \frac{6\sqrt{15} - 5}{10} \\ &= -\frac{1}{2} + \frac{3}{5}\sqrt{15} \end{aligned}$$

$$\therefore a = -\frac{1}{2}, b = \frac{3}{5}$$

7. **B** Indices (226467) **Core A**

$$\begin{aligned} \frac{(12x)^0}{4} \times \frac{5x}{3} &= \frac{1}{4} \times \frac{5x}{3} \\ &= \frac{5x}{12} \end{aligned}$$

8. **B** Cartesian Plane (228384) **Path C**

Line goes through $(-3, 4)$ and $(2, -3)$.

Using the gradient formula:

$$\begin{aligned} m &= \frac{y_2 - y_1}{x_2 - x_1} \\ &= \frac{-3 - 4}{2 - (-3)} \\ &= -\frac{7}{5} \end{aligned}$$

9. **B** Indices (005374) **Path B** **HSC**

$$\begin{aligned} \frac{4x^2}{3y} \div \frac{xy}{5} &= \frac{4x^2}{3y} \times \frac{5}{xy} \\ &= \frac{20x^2}{3xy^2} \\ &= \frac{20x}{3y^2} \end{aligned}$$

Mean mark 33%.

MARKER'S

COMMENT: Remember to "invert and multiply" when dividing a fraction by a fraction (see Worked Solution).

10. **B+** Distributive Laws (226209) **Path B**

$$\begin{aligned} -a^2 + 3a + 10 &= -(a^2 - 3a - 10) \\ &= -(a - 5)(a + 2) \\ &= (5 - a)(a + 2) \end{aligned}$$

11. **B+** Distributive Laws (226288) **Path C**

$$\begin{aligned} 5b^3 - 5b &= 5b(b^2 - 1) \\ &= 5b(b + 1)(b - 1) \end{aligned}$$

12. **B+** Indices (226472) **Path B**

$$\begin{aligned} \frac{16x^5}{2x^{-3}} &= 8x^{5-(-3)} \\ &= 8x^8 \end{aligned}$$

13. **A** Distributive Laws (226293) **Path C**

$$\begin{aligned} 2x^2 - 6xy - 3x + 9y &= 2x(x - 3y) - 3(x - 3y) \\ &= (2x - 3)(x - 3y) \end{aligned}$$

14. **A** Indices (226632) **Path B**

$$\begin{aligned} \frac{1}{a} + \frac{1}{b} - \frac{c}{ab} &= \frac{b}{ab} + \frac{a}{ab} - \frac{c}{ab} \\ &= \frac{b + a - c}{ab} \end{aligned}$$

Reciprocal of $x = x^{-1}$

$$\therefore \text{Reciprocal of } \frac{b + a - c}{ab} \Rightarrow \left(\frac{b + a - c}{ab} \right)^{-1} = \frac{ab}{a + b - c}$$